

# **Functional Analysis on the Eve of the 21st Century**

## **Volume I**

*In Honor of the Eightieth Birthday  
of I. M. Gelfand*

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