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978-0-521-86706-1 - Data Analysis Using Regression and Multilevel/Hierarchical Models

Andrew Gelman and Jennifer Hill

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