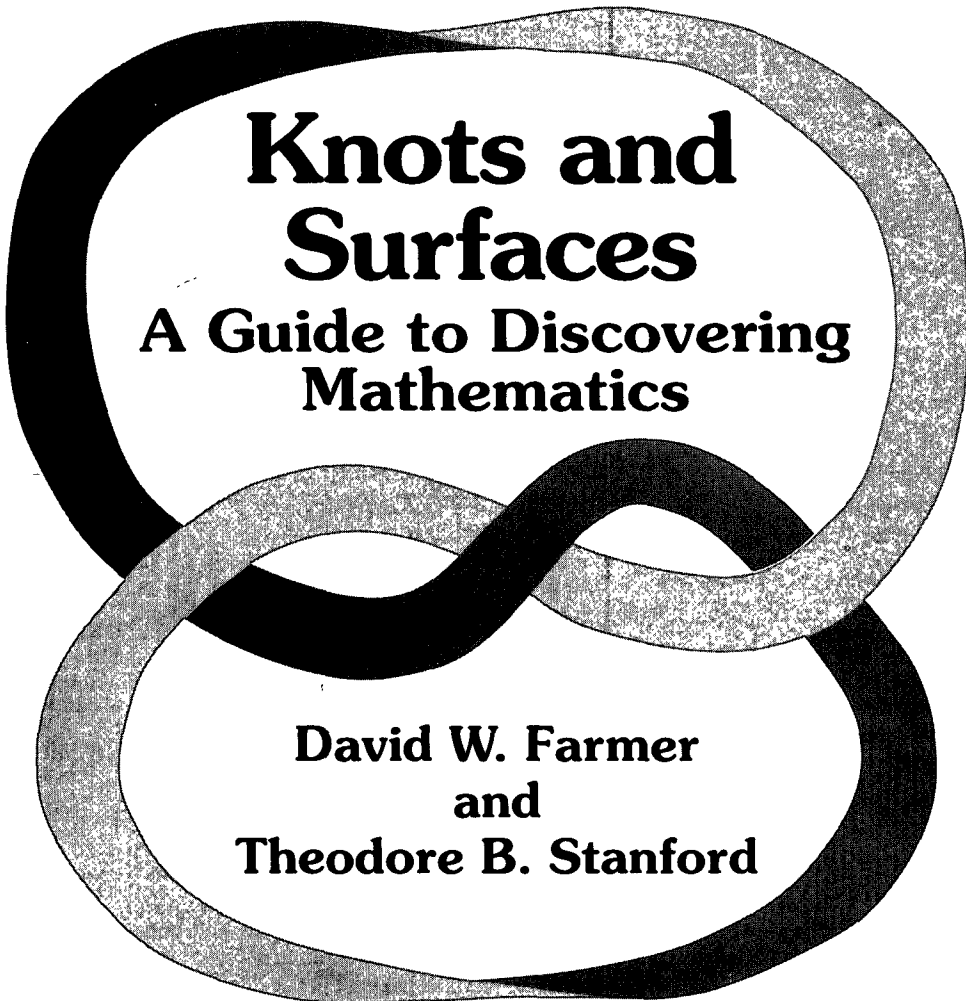


Mathematical World • Volume 6



Knots and Surfaces

A Guide to Discovering Mathematics

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American Mathematical Society

Table of Contents

Chapter 1. Networks	1
1.1 Countries of the insect world	
1.2 Notation, and a catalog	
1.3 Trees	
1.4 Trees in graphs	
1.5 Euler's formula	
1.6 Planar graphs	
1.7 Paths in graphs	
1.8 Dual graphs	
1.9 A map of the United States	
1.10 Coloring graphs	
1.11 The six-color theorem	
1.12 Notes	
 Chapter 2. Surfaces	 31
2.1 The shape of the world	
2.2 The flat torus	
2.3 Graphs on the torus	
2.4 Euler's formula, again	
2.5 Regular graphs	
2.6 More surfaces: holes	
2.7 More surfaces: connected sums	
2.8 One-sided surfaces	
2.9 Identifying two-sided surfaces	
2.10 Cell complexes	
2.11 Notes	
 Chapter 3. Knots	 59
3.1 The view from outside	
3.2 Manipulating knots	
3.3 Lots of knots	
3.4 Alternating knots	
3.5 Unknotting number	
3.6 Links	
3.7 Linking number	

3.8	Coloring knots and links	
3.9	Notes	
3.10	Catalog of knots	
Chapter 4.	Projects	87
4.1	Synthesis Projects	
	Surfaces as sculpture	
	Practical knots	
	Celtic knotwork	
	The family tree of knots	
	Graphs, knots, and surfaces in art	
	Aesthetics of graphs, knots, and surfaces	
	Illustrate a mathematical topic	
	Graphs, knots, and chemistry	
4.2	Mathematical Projects	
	Games on surfaces	
	The Double torus	
	One-sided surfaces	
	Space Tyrant mazes	
	Covering graphs	
	Knots and graphs	
	Knot polynomials	
Bibliography	97
Index	99