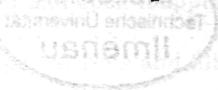


General Topology

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General Topology

Revised and completed edition



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