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978-0-521-86562-3 - Analysis of Variance and Covariance: How to Choose and Construct Models for the Life Sciences

C. Patrick Doncaster and Andrew J. H. Davey

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# Analysis of Variance and Covariance

## How to Choose and Construct Models for the Life Sciences

C. PATRICK DONCASTER and ANDREW J. H. DAVEY



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