

# Mathematical Modeling of Biological Systems, Volume I

*Cellular Biophysics, Regulatory Networks,  
Development, Biomedicine, and  
Data Analysis*

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