

**ADVANCED**

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**MATHEMATICAL &  
COMPUTATIONAL TOOLS  
IN METROLOGY VI**

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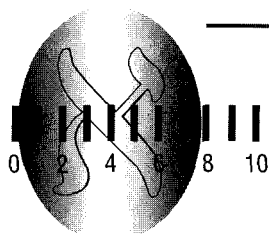
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 **World Scientific**

*Published by*

World Scientific Publishing Co. Pte. Ltd.

5 Toh Tuck Link, Singapore 596224

*USA office:* Suite 202, 1060 Main Street, River Edge, NJ 07661

*UK office:* 57 Shelton Street, Covent Garden, London WC2H 9HE

**British Library Cataloguing-in-Publication Data**

A catalogue record for this book is available from the British Library.

**ADVANCED MATHEMATICAL AND COMPUTATIONAL TOOLS  
IN METROLOGY VI**

**Series on Advances in Mathematics for Applied Sciences — Vol. 66**

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ISBN 981-238-904-0

## Contents

<i>Foreword</i>	v
Estimation of Precision and Uncertainty of a Calibration Artefact for CMMs <i>S. D. Antunes and M. A. F. Vicente</i>	1
Uncertainty in Semi-Qualitative Testing <i>W. Bremser and W. Hässelbarth</i>	16
Processing the Coherent Anomalies on Digitalized Surfaces in Wavelet Domain <i>P. Ciarlini and M. L. Lo Cascio</i>	24
Least Squares Adjustment in the Presence of Discrepant Data <i>M. G. Cox, A. B. Forbes, J. L. Flowers and P. M. Harris</i>	37
Harmonization of Correlated Calibration Curves with an Application to the Analysis of Natural Gases <i>M. G. Cox, S. Kamvissis, M. J. T. Milton and G. Vargha</i>	52
Parametrized Approximation Estimators for Mixed Noise Distributions <i>D. P. Jenkinson, J. C. Mason, A. Crampton, M. G. Cox, A. B. Forbes and R. Boudjemaa</i>	67
Algorithms for the Calibration of Laser-Plane Sensors on CMMs <i>C. Lartigue, P. Bourdet, L. Mathieu and C. Mehdi-Souzani</i>	82
Some Differences between the Applied Statistical Approach for Measurement Uncertainty Theory and the Traditional Approach in Metrology and Testing <i>C. Perruchet</i>	98
Metrology Software for the Expression of Measurement Results by Direct Calculation of Probability Distributions <i>G. B. Rossi, F. Crenna and M. Codda</i>	106

Feasibility Study of Using Bootstrap to Compute the Uncertainty Contribution from Few Repeated Measurements <i>B. R. L. Siebert and P. Ciarlini</i>	122
Recursive and Parallel Algorithms for Approximating Surface Data on a Family of Lines or Curves <i>G. Allasia</i>	137
Process Measurement Impact on the Verification Uncertainty <i>J. Bachmann, J. M. Linares, S. Aranda and J. M. Sprauel</i>	149
On the In-Use Uncertainty of an Instrument <i>W. Bich and F. Penneccchi</i>	159
Automatic Differentiation and Its Application in Metrology <i>R. Boudjemaa, M. G. Cox, A. B. Forbes and P. M. Harris</i>	170
Usage of Non-Central Probability Distributions for Data Analysis in Metrology <i>A. Chunovkina</i>	180
Implementation of a General Least Squares Method in Mass Measurements <i>J. Hald and L. Nielsen</i>	189
The GUM Tree Design Pattern for Uncertainty Software <i>B. D. Hall</i>	199
Statistical Hypotheses Testing for Phase Transition Identification in Cryogenic Thermometry <i>D. Ichim, I. Peroni and F. Sparasci</i>	209
The Impact of Entropy Optimization Principles on the Probability Assignment to the Measurement Uncertainty <i>G. Iuculano, A. Zanobini and G. Pellegrini</i>	219
Stochastic Processes for Modelling and Evaluating Atomic Clock Behaviour <i>G. Panfilo, P. Tavella and C. Zucca</i>	229
Compound-Modelling of Metrological Data Series <i>F. Pavese</i>	240

Homotopic Solution of EW-TLS Problems <i>M. L. Rastello and A. Premoli</i>	251
Pooled Data Distributions: Graphical and Statistical Tools for Examining Comparison Reference Values <i>A. G. Steele, K. D. Hill and R. J. Douglas</i>	264
Numerical Uncertainty Evaluation for Complex-Valued Quantities: A Case Example <i>L. Callegaro, F. Pennechi and W. Bich</i>	274
Bayesian Approach to Quantum State Tomography <i>S. Castelletto, I. P. Degiovanni, M. L. Rastello and I. Ruo Berchera</i>	279
Simulation of Charge Transfer in a Tunnel Junction: Approaching the Sub- $e$ Scale <i>G. E. D'Errico</i>	282
Validation of Calibration Methods — A Practical Approach <i>E. Filipe</i>	285
Comparison of LS Techniques for the Linear Approximation of Data Affected by Heteroschedastic Errors in Both Variables with Uncertainty Estimation <i>D. Ichim, P. Ciarlini, F. Pavese, A. Premoli and M. L. Rastello</i>	293
Noise Correction for Surface Measurements <i>H. Haitjema and M. A. A. Morel</i>	299
Evaluation of Uncertainty of Standard Platinum Resistance Thermometer at National Laboratory Level <i>M. J. Korczynski, A. Hetman, A. Szmyrka-Grzebyk and P. Fotowicz</i>	302
A New Approach to the Presentation of the Result Measurements in Virtual Instruments <i>M. J. Korczynski and A. Hetman</i>	309
A Hybrid Method for $\ell_1$ Approximation <i>D. Lei and J. C. Mason</i>	314

Interpolation Equations for Industrial Platinum Resistance Thermometers <i>P. Marcarino, P. P. M. Steur and A. Merlone</i>	318
From the Fixed Points Calibration to the Certificate: A Completely Automated Temperature Laboratory <i>A. Merlone, P. Marcarino, P. P. M. Steur and R. Dematteis</i>	323
A New Off-Line Gain Stabilisation Method Applied to Alpha-Particle Spectrometry <i>S. Pommé and G. Sibbens</i>	327
Development of Software for ANOVA that Can Generate Expressions of Variance Expectations <i>H. Tanaka, T. Kamoshita and K. Ehara</i>	330
Template Matching in Passive Sonar Recognition <i>J. L. Terry, D. A. Turner and J. C. Mason</i>	333
Fast Computational Alternative to Monte Carlo Simulation of an Output Distribution <i>R. D. Willink and B. D. Hall</i>	337
<i>Short Course on Uncertainty Evaluation</i> <i>M. G. Cox</i>	342
<i>Software Requirements in Legal Metrology: Short Course Held Adjacent to the Conference</i> <i>D. Richter</i>	345
<i>Author Index</i>	349