

Nicolas Bouleau

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# Financial Markets and Martingales

**Observations on Science and Speculation**

Translated by Alan Thomas

With 14 Illustrations



Springer

Nicolas Bouleau, PhD, Alumnus of the École Polytechnique  
École des Ponts, 28 rue des Saint Pères, 75007 Paris, France

*Translator*

Alan D. Thomas

Department of Mathematics, University of Wales Swansea, Singleton Park, Swansea,  
SA2 8PP, Wales, UK

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