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# A. ADRIAN ALBERT

COLLECTED  
MATHEMATICAL PAPERS

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Part 2

## Nonassociative Algebras and Miscellany

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