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052160415X - Advances in Elliptic Curve Cryptography

Edited by Ian F. Blake, Gadiel Seroussi and Nigel P. Smart

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