
Wolfgang Demtröder

Atoms, Molecules and Photons

An Introduction to Atomic-, Molecular-
and Quantum Physics

Third Edition

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