

L. Ambrosio · N. Dancer

# Calculus of Variations and Partial Differential Equations

Topics on  
Geometrical Evolution Problems  
and Degree Theory

Edited by G. Buttazzo, A. Marino,  
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Springer

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