## Studies in Economic Theory

### Editors

Charalambos D. Aliprantis Department of Mathematics IUPUI 1125 E 38th Street Indianapolis, IN 46205-2810 USA

Nicholas C. Yannelis Department of Economics University of Illinois Champaign, IL 61820 USA



### Titles in the Series

M. Ali Khan and Nicholas C. Yannelis (Eds.) Equilibrium Theory in Infinite Dimensional Spaces Charalambos D. Aliprantis · Kim C. Border Wilhelmus A. J. Luxemburg

# Positive Operators, Riesz Spaces, and Economics

Proceedings of a Conference at Caltech, Pasadena, California, April 16-20, 1990

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Charalambos Aliprantis Department of Mathematics IUPUI 1125 East 38th Street Indianapolis, IN 46205-2810 USA

Kim C. Border Division of Humanities and Social Sciences California Institute of Technology Pasadena, CA 91125 USA

Wilhelmus A. J. Luxemburg Department of Mathematics California Institute of Technology Pasadena, CA 91125 USA

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## Foreword

Over the last fifty years advanced mathematical tools have become an integral part in the development of modern economic theory. Economists continue to invoke sophisticated mathematical techniques and ideas in order to understand complex economic and social problems. In the last ten years the theory of Riesz spaces (vector lattices) has been successfully applied to economic theory. By now it is understood relatively well that the lattice structure of Riesz spaces can be employed to capture and interpret several economic notions.

On April 16–20, 1990, a small conference on Riesz Spaces, Positive Operators, and their Applications to Economics took place at the California Institute of Technology. The purpose of the conference was to bring mathematicians specialized in Riesz Spaces and economists specialized in General Equilibrium together to exchange ideas and advance the interdisciplinary cooperation between mathematicians and economists. This volume is a collection of papers that represent the talks and discussions of the participants at the week-long conference.

We take this opportunity to thank all the participants of the conference, especially those whose articles are contained in this volume. We also greatly appreciate the financial support provided by the California Institute of Technology. In particular, we express our sincerest thanks to David Grether, John Ledyard, and David Wales for their support.

Finally, we would like to thank Susan Davis, Victoria Mason, and Marge D'Elia who handled the delicate logistics for the smooth running of the conference.

June, 1991

C. D. Aliprantis, K. C. Border, and W. A. J. Luxemburg

# Contents

Foreword	v
Valuation and Optimality in Exchange Economies with a Countable Number of Agents C. D. Aliprantis, D. J. Brown, and O. Burkinshaw	1
Equilibrium Points of Non-Cooperative Random and Bayesian Games N. C. Yannelis and A. Rustichini	23
Equilibria of Large Games with Imperfect Observability S. K. Chakrabarti and M. A. Khan	49
Functional Analytic Tools for Expected Utility Theory K. C. Border	69
<b>Remarkable Points and </b> $X_{(N)}$ <b>-spaces</b> Y. A. Abramovich	89
Integration with Respect to Finitely Additive Measures W. A. J. Luxemburg	109
Lattice-Ordered Algebras and <i>f</i> -Algebras: A Survey C. B. Huijsmans	151
Approximating Derivative Securities in <i>f</i> -Algebras D. J. Brown, C. B. Huijsmans, and B. de Pagter	171
Some Unpleasant Objects in a Non-separable Hilbert Space M. A. Khan and A. Rustichini	179
The Hopf Decomposition in Riesz Spaces R. Zaharopol	189
Frobenius Decomposition of Positive Compact Operators R. Jang and H. D. Victory, Jr.	195
Irreducible Positive Operators and Hyperinvariant Ideals Y. A. Abramovich, C. D. Aliprantis, and O. Burkinshaw	225