

THE CONSISTENCY OF THE
AXIOM OF CHOICE AND OF THE
GENERALIZED CONTINUUM-HYPOTHESIS
WITH THE AXIOMS OF SET THEORY

BY

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In the second and subsequent printings a few misprints and minor inaccuracies have been corrected. Note in particular the references to the highly important developments in the foundations of set theory that have occurred since 1960.

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